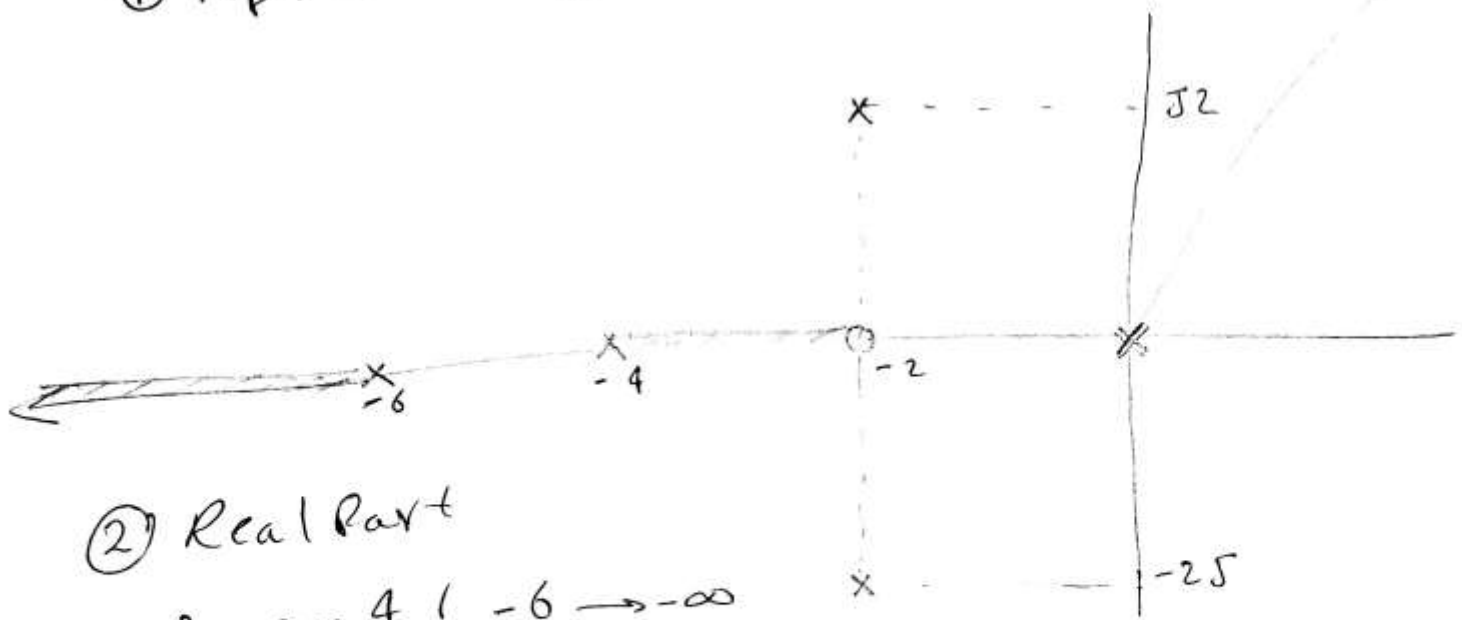


Control sec 4

$$GH(s) = \frac{K(s+2)(s+6)}{s^2(s+4)(s^2+4s+8)}$$

① $n_p = 5$ & $n_z = 2$



② Real Part

$$-2 \rightarrow -4 \mid -6 \rightarrow -\infty$$

③ Asymptotes

$$n_o = 5 - 2 = 3$$

$$C_A = \frac{(0 + 0 - 2 + 2j - 2 - 2j - 4 - 6) - (-2)}{3} = \frac{-12}{3} = -4$$

$$\theta = \frac{(2L + 1) \times 180^\circ}{3} = (2L + 1) 60^\circ$$

$$\ominus \rightarrow \begin{cases} 60^\circ \\ 180^\circ \end{cases}$$

④ Breaking points

Breaking in: ∞ (zeros) بين

$$K = \frac{-1}{GH(s)} \Rightarrow \frac{-s^2 (s+4) (s^2+4s+8)}{(s+2)(s+6)}$$

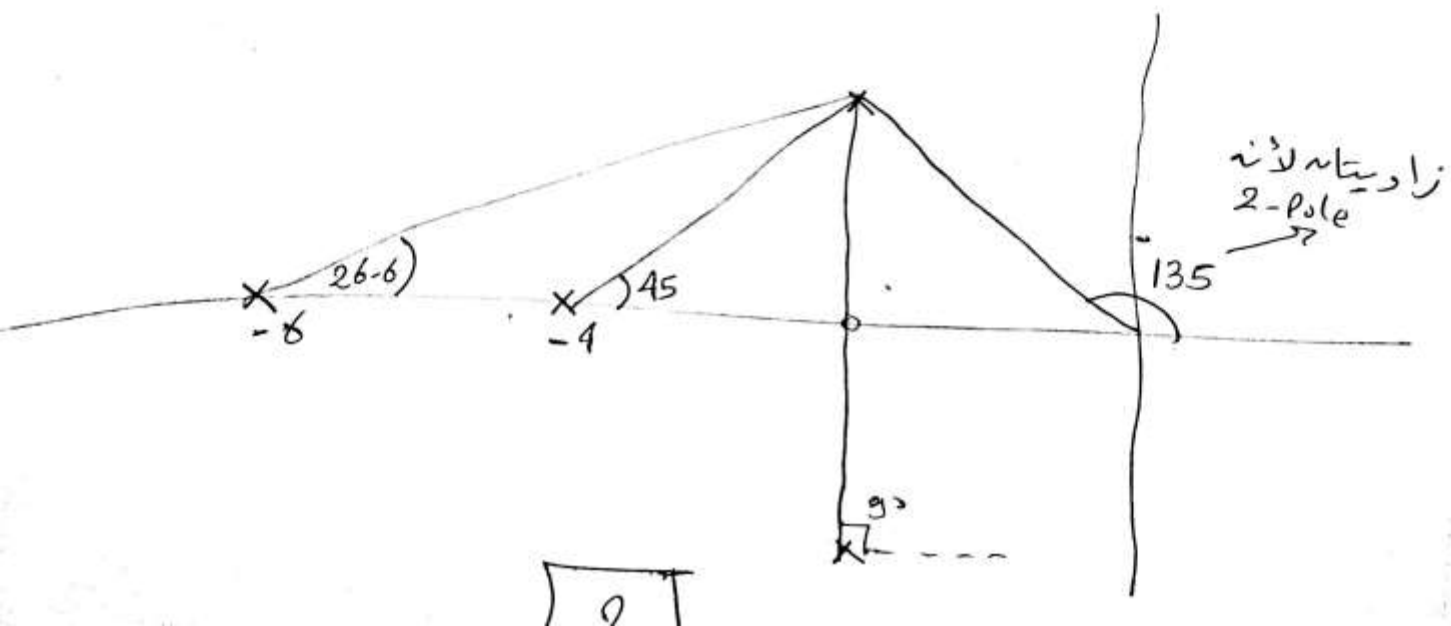
s	-6	-6-5	-7	...
K				

K = min

← فنحن نقيم الجذور حتى نصل لقيمة تزيد عن 0 قيمة
K فنحن K min

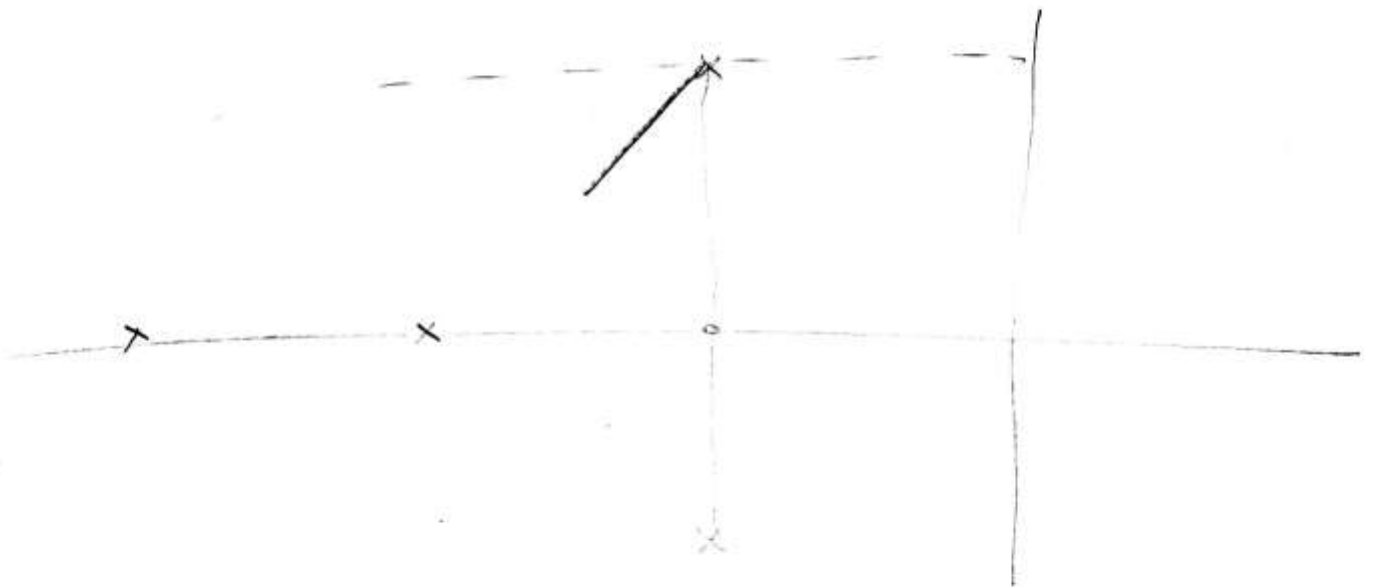
⑤ Departure Angle.

$$D = 180 - \phi_p + \phi_z$$



$$\phi_a \approx 180 - (135 + 135 + 135) + 90 + 26.6$$

$$= -108.4$$



⑥ Range of K for stability (Routh)

$$1 + KGH(s) = 0$$

$$s^2(s+4)(s^2+4s+8) + K(s^2+8s+12) = 0$$

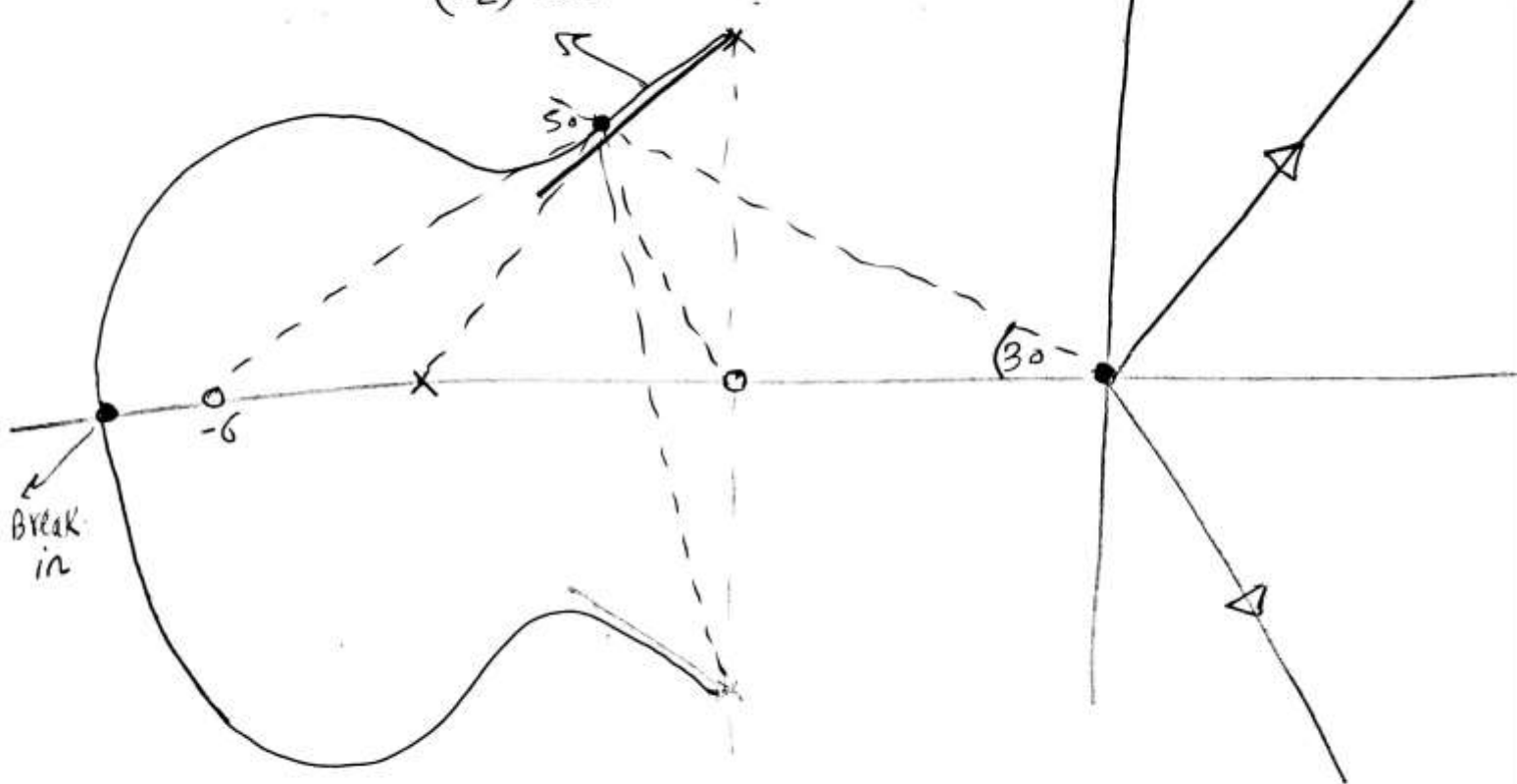
$$s^5 + 8s^4 + 12s^3 + (32+K)s^2 + 8Ks + 12K = 0$$

→ Range of K .

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(Zero) \rightarrow خط بسبب ال
 $(-2) \text{ is}$

$t_s \geq 4$ $t_s = 4$ $t_s < 4$



Required

$$\zeta = \frac{\sqrt{3}}{2} \quad t_s \leq 4$$

$$\rightarrow \theta = \cos^{-1} \zeta = \cos^{-1} \frac{\sqrt{3}}{2} = 30$$

$$K|_{s_0} = \frac{\pi \text{ Poles}}{\pi \text{ Zeros}}$$

$$t_s = \frac{4}{\omega_n} = 4 \quad \omega_n = 1$$

①

$$\Rightarrow \text{num} = [1 \quad 8 \quad 12];$$

$$\Rightarrow \text{den} = \text{conv}(\text{conv}[1 \ 0 \ 0], [1 \ 4 \ 8], [1 \ 4]);$$

$$\Rightarrow G = \text{tf}(\text{num}, \text{den});$$

$$\Rightarrow \text{rlocus}(G).$$

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